Nationale Wiskunde Dagen

Chocolate Bar Machine Scheduling: Dunking into Inquiry-Based Learning and the World of Work

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The mascil Framework



Valued outcomes

- Inquiring minds
- Applying science in real life
- Preparing for active citizenship and lifelong learning
- Understanding the nature of science
- Understanding how mathematics and science are used in the World of Work

What students do

- Inquire, pose questions
- Explore problems, engage in solving them. use their knowledge to find solutions
- Explain situations and phenomena
- Reflect on the results and processes - Make sense for themselves
- Explore the World of Work



Teacher guidance

- Values and builds upon pupils' reasoning and reflections
- Connects to pupils' experience
- Motivates students by connecting
- school and work

Classroom culture

- Shared sense of purpose/justification
- Value mistakes, contributions (open-minded)
- Dialogic
- Shared ownership
- Collaborative

IBL tasks

- The context is meaningful
- The situation evokes multiple solution strategies
- The students plan inquiry
- The task supports collaboration and communication

World of Work

- The context of the task relates to the WoW
- Students have to take a professional role
- Students' activities reflect workplace practices
- The task asks for a product

Dunking into IBT and WoW



Chocolate Bar Machine Scheduling

special task to provide a fast and effective tool involving pre-service and in-service mathematics teachers in a mascil learning environment

Chocolate Bar Machine Scheduling

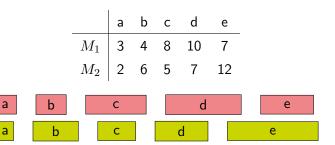


Introduction

Chocolate Bar Machine Scheduling



A chocolate factory produces different sorts of chocolate bars (hazelnuts, nougat, milk ...). For each sort, the melted chocolate is deposited into bars on a machine M_1 and then the bars are packed on a machine M_2 . The processing times of five sorts a,b,c,d,e on each machine are given.



For which order of the sorts is the total processing time – the interval between the time the first sort starts on machine M_1 and the time the last sort leaves machine M_2 – the shortest? Describe your ideas and strategies!

Planning in een chocoladefabriek



Een chocoladefabriek produceert verschillende soorten chocoladerepen (melk, puur, hazelnoot, ...). Van iedere soort wordt de gesmolten chocola met machine M_1 in reepvormen gegoten en daarna wordt met machine M_2 de reep ingepakt. De tijd die de machines nodig hebben voor vijf verschillende soorten chocola a,b,c,d,e en f zijn hieronder gegeven.

			а	b	С	d	е		
		M_1	3	4	8	10	7		
		M_2	2	6	5	7	12		
а	b		С			d		е	
а	b		С		(d		е	

Voor welke volgorde van de vijf soorten is de totale verwerkingstijd – de tijd tussen het moment waarop de eerste soort start op machine M_1 en het moment waarop de laatste soort ingepakt is in machine M_2 – het kortste? Beschrijf je ideeën en de manier waarop je het probleem hebt aangepakt.

Chocolate Bar Machine Scheduling



Discussion

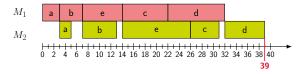
Intuitive Approach



Hypothesis: "the shortest first"

- 1. Sort all jobs in ascending order with respect to their processing time at machine ${\cal M}_1$.
- 2. Schedule the jobs in this order.

For our task:



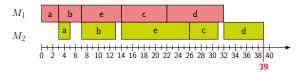
Intuitive Approach



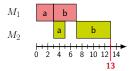
Hypothesis: "the shortest first"

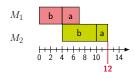
- 1. Sort all jobs in <u>ascending</u> order with respect to their processing time at machine M_1 .
- 2. Schedule the jobs in this order.

For our task:



Counterexample to the hypothesis:





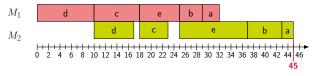
Inverse Intuitive Approach



Hypothesis: "the longest first"

- 1. Sort all jobs in descending order with respect to their processing time at machine M_1 .
- 2. Schedule the jobs in this order.

For our task:



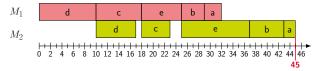
Inverse Intuitive Approach



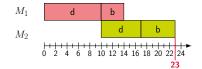
Hypothesis: "the longest first"

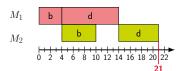
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- 2. Schedule the jobs in this order.

For our task:



Counterexample to the hypothesis:





Johnson's rule



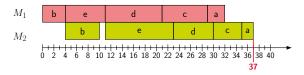
- 1. List the jobs and their processing times at each machine.
- 2. Select the job with the shortest processing time. If this processing time is at machine M_1 , then schedule the job first. If this processing time is at machine M_2 then schedule the job last. In the case of ties, select the first listed job. In the case of ties between the processing time at machine M_1 and machine M_2 schedule the job first.
- 3. Eliminate the shortest job from further consideration.
- 4. Repeat steps 2 and 3, working towards the center of the job schedule until all jobs have been scheduled.

Johnson's rule



	а	b	С	d	е
M_1	3	4	8	10	7
M_2	2	6	5	7	12

For our task:







Introduction of the task







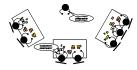
Introduction of the task

Development of the task









Introduction of the task

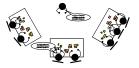
Development of the task

Discussion of the task











Introduction of the task

Development of the task

Discussion of the task

Systematization of the mathematical learning

Teacher's Questioning in IBMT



Menezes et al., 2013

	PHASES OF AN INQUIRY-BASED MATHEMATICS LESSON				
TEACHER'S QUESTIONS	Introduction of the task	Development of the task	Discussion of the task	Systematization of mathematical learning	
Verification					
Focusing					
Inquiry					

figure i – the teacher's questions in an inquiry-based mathematics lesson

Quelle: Menezes et al., 2013: Essay on the role of teacher's questioning in inquiry-based mathematics teaching, p. 69

Teacher's Questioning in IBMT



Menezes et al., 2013

PHASES OF AN INC	QUIRY-BASED	MATHEMATICS	LESSON
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TEACHER'S QUESTIONS	Introduction of the task	Development of the task	Discussion of the task	Systematization of mathematical learning
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Inquiry				

figure I - the teacher's questions in an inquiry-based mathematics lesson

Quelle: Menezes et al., 2013: Essay on the role of teacher's questioning in inquiry-based mathematics teaching, p. 69

Teacher's Questioning in IBMT





PHASES OF AN INQUIRY-BASED MATHEMATICS LESSON

TEACHER'S QUESTIONS	Introduction of the task	Development of the task	Discussion of the task	Systematization of mathematical learning
Verification				
Focusing				
Impulma				_
Inquiry				

FIGURE I - THE TEACHER'S QUESTIONS IN AN INQUIRY-BASED MATHEMATICS LESSON

Quelle: Menezes et al., 2013: Essay on the role of teacher's questioning in inquiry-based mathematics teaching, p. 69



Teacher's Questions

- Verification
- Focusing
- Inquiry



Teacher's Questions

- Verification
- Focusing
- Inquiry

"Do you always start with job A?"



Teacher's Questions

- Verification
- Focusing
- Inquiry

"Do you have an example in which it [the hypothesis that one should start with the shortest job] is wrong?"



Teacher's Questions

- Verification
- Focusing
- Inquiry

"It is difficult [to start] with [a job in] the middle if you have many [jobs]. But why do you believe that this [job] is in the front and that [job] at the end?"



Teacher's Questions

■ Verification 14% (9)

■ Focusing 32% (21)

■ Inquiry 54% (35)



mascil framework



- mascil framework
- worked on a mascil task



- mascil framework
- worked on a mascil task
- different approaches



- mascil framework
- worked on a mascil task
- different approaches
- implementation (different phases)



- mascil framework
- worked on a mascil task
- different approaches
- implementation (different phases)
- teacher's questioning



- mascil framework
- worked on a mascil task
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- implementation (different phases)
- teacher's questioning

... comments?

Further Information



Websites

■ international: http://www.mascil-project.eu/

■ subwebsite NL: http://www.projects.science.uu.nl/Mascil/

Contact

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Thank you for your attention.