# Voorbeelden van opgaven voor een mondeling eindexamen Meike Akveld, Januari 2011

# 1. Vector Geometry

Suppose we define a new product for vectors by

$$\mathbf{u} * \mathbf{v} = -\frac{1}{2} \, \mathbf{u} \times \mathbf{v}$$

Here  $\times$  denotes the normal vector product.

- (a) What sort of object is  $\mathbf{u} * \mathbf{v}$ ?
- (b) Can you give three geometric properties of this new product?

## 2. Vector Geometry

Consider the equation

$$3x + 2y - z = 6$$

- (a) What is the geometric interpretation of this equation?
- (b) Can you find the parametrised equation of this plane?
- (c) Suppose we substitute one of the parameters, say t, by  $\sin t$ . What is now parametrised?
- (d) And what if we substitute the other parameter, say s, by  $e^s$ ?

#### 3. Analysis

Consider the functions f(x) = 2x + 1 and  $g(x) = \frac{1}{x}$ .

- (a) What can you say about these functions?
- (b) Determine  $f \circ g$  and  $g \circ f$ .
- (c) Determine  $f \circ f$ ,  $f \circ f \circ f$  and  $f^{(n)}$  can you prove this?
- (d) The same for g.

#### 4. Analysis

- (a) What do mathematicians mean by  $\mathbb{Z}$ ?
- (b) Can you name two integers whose product is equal to their sum.
- (c) Are there any other such integers? Can you express this relation with an equation solve it for y
- (d) What sort of function is this? Graph?
- (e) Can we now answer the original question for certain?

## 5. Vector Geometry and Combinatorics

- (a) Can you explain what is meant by the following notation  $\begin{pmatrix} 1 \\ 2 \\ 3 \end{pmatrix}$ ?
- (b) Can you give another vector of the same length? Any more with integer coefficients?
- (c) If we just permute these three components, how many different vectors do you get?
- (d) Seen as position vectors, where do the endpoints lie, and why? (circle on sphere of radius  $\sqrt{14}$ )